

### Extra information not in official formula sheets

In the official formula sheets you need to become familiar with all the symbols and equations used.

## VCE Mathematical methods

## HSC Mathematics

## AISSE Mathematics

### Algebra:

$$(a + b)^2 = a^2 + 2ab + b^2$$

$$a^2 - b^2 = (a - b)(a + b)$$

Solve $ax^2 + bx + c = 0$	$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
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$$1 = 0! = 0^0 = 1^0$$

Binomial theorem  $k^{\text{th}}$  term of  $(a + b)^n$  is  $C_k^n a^{n-k} b^k$  for  $k = 0, 1, \dots, n$ .

$$\log_e(x) = \ln(x) = \ln x = \text{natural log of } x$$

$$\log_a(b) = \log_e(b)/\log_e(a)$$

Surd: irrational number e.g.  $\sqrt{2}$

### Geometry:

Sides of simple right-angled triangles:

3, 4, 5

5, 12, 13

7, 24, 25

$1/\sqrt{2}, 1/\sqrt{2}, 1$

1,  $\sqrt{3}, 2$

$$\sec(x) = 1/\cos(x)$$

$$\operatorname{cosec}(x) = 1/\sin(x)$$

$$\cot(x) = 1/\tan(x)$$

Rule for positive result in quadrant (start at top right and rotate anti-clockwise):

ASTC: all science teachers count. (meaning all, sine, tangent, cosine)

Surface area of sphere:  $4\pi r^2$

Area of a triangle given vertex coordinates:  $(1/2) | a_x(b_y - c_y) + b_x(c_y - a_y) + c_x(a_y - b_y) |$

### Statistics:

Approximate % for  $\Pr(X)$  within 1, 2 or 3 standard deviations: 68, 95, 99.7 .

Binomial formula term.  $C_n^N p^n (1 - p)^{N-n}$

Binomial distribution.  $\mu = np$   $\text{var} = np(1 - p) = \sigma^2$

$C_n^N = (N!) / (n! (N-n)!) =$  number of ways of choosing  $n$  from  $N$  when order is unimportant such as cards.

$(n!) C_n^N = (N!) / (N-n)! =$  number of ways of choosing  $n$  from  $N$  when order is important such as a race.

Z-score = standardised score =  $(x - \mu) / \sigma$

## VCE Further Mathematics

Residual = actual – predicted.

Bearing is measured anticlockwise in degrees.

### Networks and decision maths

In Euler's formula:  $v =$  vertices,  $f =$  faces,  $e =$  edges.

For triangle:  $v + f = e + 2$  becomes  $3 + 2 = 3 + 2$ . The triangle has 2 faces: inside and outside.

Euler path: must include every edge just once.

Hamiltonian circuit: goes through each vertex only once and ends at start.

Degree of a vertex = number of edges. For a loop both ends count.

Degree of a graph = largest vertex degree.

### Correlation:

Correlation =  $r =$  Pearsons correlaton = Pearsons product-moment correlation. (Range -1 to 1)

$$r = \frac{n(\sum xy) - (\sum x)(\sum y)}{\sqrt{[n\sum x^2 - (\sum x)^2][n\sum y^2 - (\sum y)^2]}}$$

Coefficient of determination =  $r^2$

### Series:

Arithmetic series:  $a + (a + d) + \dots + (a + (n - 1)d) = (n/2)[2a + (n - 1)d] = (n/2)(a + l)$

Geometric series:  $a + ar + ar^2 + \dots + ar^{(n - 1)} = a(1 - r^n)/(1 - r)$ ,  $r$  not equal 1.

Infinite geometric series:  $a + ar + ar^2 + \dots = a/(1 - r)$ ,  $|r| < 1$ .

### geometry and trigonometry

Pythagoras theorem  $c^2 = a^2 + b^2$

### business-related mathematics

$R =$  annual interest rate

$N =$  payments/year

$P =$  principal

$T =$  time in years

I = interest paid  
 Simple interest:  $I = PRT/100$   
 Compound interest:  $I = P (1 + R/(100N))^{NT} - P$   
 Hire purchase:  
 $r_f = (100 I M)/(PN)$  = flat rate of interest paid for hire purchase  
 I = total interest paid = repayments – principal repayments  
 P = principal – deposit  
 M = number of repayments/year  
 N = total number of repayments or periods  
 $r_e = r_f (2N)/(2N + 1)$  = effective rate of interest

## VCE Physics

Photon energy  $E = hf = hc/\lambda$

Relativistic mass  $m = m_0 \gamma$  ( $\gamma$  always  $>1$ )

Total energy as seen by observer  $E_{\text{total}} = E_k + E_{\text{rest}} = mc^2$

Time dilation  $t = t_0 \gamma$   $t_0$  = proper time of observed.  $t$  = time for observer.

Length contraction  $L = L_0 / \gamma$   $L_0$  = proper length of observed.  $L$  = length for observer.

Stress  $\sigma = F/A$

Strain  $\epsilon = (\Delta L)/L$

Young's modulus  $E = \text{stress/strain}$

Capacitor time constant  $\tau = R C$

### Extra data:

Mass of proton  $m_p = 938.3 \text{ MeV}$  equivalent energy or  $\text{MeV}/c^2$   
 Mass of neutron  $m_n = 939.6 \text{ MeV}$  equivalent energy or  $1.675 \times 10^{-27} \text{ kg}$   
 Speed of sound in air  $340 \text{ m/s}$